



## PHYSICAL SCIENCES

Paper - II

1. A force $f$ acting on a particle is proportional to velocity gradient. The law is given by $f=\mu \frac{d u}{d x}$ where $u$ is velocity of the particle, x is distance travelled and $\mu$ is the proportionality constant. The dimensions of $\mu$ are
(A) $\mathrm{ML}^{-1} \mathrm{~T}$
(B) $\mathrm{MLT}^{-1}$
(C) $\mathrm{M}^{-1} \mathrm{~L}^{-1} \mathrm{~T}$
(D) $\mathrm{ML}^{-1} \mathrm{~T}^{-1}$
2. If $r=x i+y j+z k$ and $a$ is a constant vector,

## Column I

## Column II

I. $\nabla \times(a \times r)$

1. -2 a
II. $(a \times \nabla) \times r$
2. $2(r \times a)$
III. $a \times(\nabla \times r)$
3. 2 a
IV. $\nabla \times($ (r.r)a)
4. 0

Choose correct matching among A, B, C, D for the row I, II, III, IV given below

| I | II | III | IV |
| :---: | :---: | :---: | :---: |
| (A) 3 | 4 | 2 | 1 |
| (B) 3 | 1 | 4 | 2 |
| (C) 2 | 3 | 4 | 1 |
| (D) 4 | 3 | 1 | 2 |

3. If det $A \neq 0$, which of the following is NOT true?
(A) $A$ is singular
(B) $A x=b$ will have unique solution
(C) A has non zero eigen values
(D) All columns of A are independent
4. If a square matrix A is singular, then which of the following is true?
(A) Modulus of eigen values $=1$
(B) Coefficient of $\lambda$ in the characteristic polynomial $=0$
(C) Constant term of characteristic polynomial $=0$
(D) Sum of the eigen values is zero.
5. If $y_{1}, y_{2}, \ldots, y_{n}$ are solutions of $n^{\text {th }}$ order differential equation and sum of the solutions i.e $\sum y_{i}$ is also a solution of the differential equations, then the differential equation is
(A) linear and homogeneous
(B) linear and non-homogeneous
(C) nonlinear and homogeneous
(D) homogeneous
6. Assertion (A) : If $X$ is a normal random variable, then mean is zero.

Reason (R): Square of the standard deviation is equal to second moment about mean.
(A) Both A and R are true
(B) $A$ is false but $R$ is true
(C) $A$ is true but $R$ is false
(D) $A$ is true but $R$ is not correct explanation
7. The probability that $A$ passes a test is $1 / 5$, the probability that $B$ passes the same test is $2 / 3$. The probability that only one of them passes is
(A) $3 / 5$
(B) $2 / 15$
(C) $13 / 15$
(D) $4 / 15$
8. If $w=f(z)$ is analytic, then
(A) $\frac{\partial w}{\partial z}=\frac{\partial w}{\partial \bar{z}}$
(B) $\frac{\partial w}{\partial z}=0$
(C) $\frac{\partial w}{\partial \bar{z}}=0$
(D) $\frac{\partial w}{\partial z}=i \frac{\partial w}{\partial \bar{z}}$
9. $\int_{0}^{1} x J_{n}(\alpha x) J_{n}(\beta x) d x=0$ if
(A) $\alpha \neq \beta$
(B) n is integer only
(C) $\alpha, \beta$ are integers only
(D) $0<\alpha, \beta<1$
10. Newton's laws are not valid if
(A) Bodies are in contact with each other
(B) Observers are moving at constant velocity
(C) Reference frame is at rest or fixed
(D) Reference frame is rotating
11. In phase space diagram of a dynamical system, a point represents, if $\mathrm{n}=\mathrm{df}$
(A) n , momentum coordinates $\mathrm{p}_{\mathrm{i}}$
(B) $n$, generalise coordinates $q_{i}$
(C) 2 n momentum and generalise coordinates $\left(p_{i}, q_{i}\right)$
(D) 2 n space and rotation coordinates
12. In phase space, $\qquad$ is invariant under canonical transformations.
(A) momentum
(B) energy
(C) angular velocity
(D) volume
13. A particle is moving on elliptical path under inverse square law of force of the form $f=-k / r^{2}$. Which of the following statements are true? The eccentricity of the orbit is
l. Function of total energy
II. Independent of total energy
III. Function of angular momentum
IV. Independent of angular momentum
(A) I, III are true
(B) I, II are true
(C) II, IV are true
(D) I, IV are true
14. Rutherford's differential scattering crosssection
(A) has the dimensions of area
(B) has the dimensions of solid angles
(C) is proportional to the kinetic energy of the incident particle
(D) inversely proportional to $\cos \phi, \phi$ is the scattering angle
15. Choose the correct statement.
I. In $\delta$ variation, time and space coordinates vary
II. In $\Delta$ variation, time and space coordinates vary
III. $\delta$ variation is independent of time
IV. $\Delta$ variation is independent of time
(A) I, IV are true
(B) II, III are true
(C) I, II are true
(D) III, IV are true
16. Which of the following is NOT a Kepler's law?
(A) All planets move in plane curves
(B) The radius vector of the planet sweeps equal areas in equal intervals of times
(C) Cube of the time period of the planet is proportional to square of the area traced
(D) Angular momentum of the planet is always constant
17. For a cyclic ordinate of the Lagrangian of the system, the corresponding
(A) momentum is constant
(B) energy is constant
(C) force is constant
(D) torque is constant
18. In the laboratory a particle $A$ has velocity v , another particle $B$ has velocity -v , the velocity of $A$ relative to $B$ is
(A) 2 v
(B) $2 v /\left(1+v^{2} / c^{2}\right)$
(C) $2 v /\left(1-v^{2} / c^{2}\right)$
(D) $2 v / \sqrt{ }\left(1-v^{2} / c^{2}\right)$
19. Div $\overline{\mathrm{D}}$ has a value wherever
i. Electric charge is present
ii. Magnetic dipole is present
(A) i is correct and ii is wrong
(B) ii is correct and i is wrong
(C) Both i and ii are correct
(D) Both i and ii are wrong
20. In a homogeneous and isotropic media $\overline{\mathrm{D}}$ and $\overline{\mathrm{E}}$ are
(A) In the same direction
(B) In the opposite direction
(C) Perpendicular to each other
(D) May be in different orientation
21. The intrinsic resistance of empty space is given by
(A) $\sqrt{\varepsilon_{0} / \mu_{0}}$
(B) $\sqrt{\mu_{0} / \varepsilon_{0}}$
(C) $\varepsilon_{0} / \mu_{0}$
(D) $\left(\varepsilon_{0} / \mu_{0}\right)^{2}$
22. Choose the correct statement.
i. In a lossless nondispersive media the group velocity is always greater than phase velocity.
ii. In a dispersive medium, the phase velocity is a function of frequency and hence of the free space wavelength.
(A) i is correct and ii is wrong
(B) ii is correct and i is wrong
(C) Both i and ii are correct
(D) Both i and ii are wrong
23. Poisson's equation in charge free space reduces to
(A) Laplace's equation
(B) Gauss's law for dielectrics
(C) Kirchoff's law
(D) Lorentz's force equation
24. Three point charges $30 \mu \mathrm{C}, 130 \mu \mathrm{C}$ and $-80 \mu \mathrm{C}$ are enclosed by a surface. The net flux across the surface is
(A) $-50 \mu \mathrm{C}$
(B) $60 \mu \mathrm{C}$
(C) $80 \mu \mathrm{C}$
(D) $-80 \mu \mathrm{C}$
25. Choose the correct statement.
i. The divergence of a curl for any vector field is the zero scalar.
ii. The curl of a gradient for any scalar function of position is the zero vector.
(A) $i$ is correct and ii is wrong
(B) ii is correct and $i$ is wrong
(C) Both i and ii are correct
(D) Both i and ii are wrong
26. Assertion (A): Bar magnet freely dropped through a long copper conduit held vertically moves with terminal velocity.

Reason (R): This is a consequence of Kirchoff's law.
(A) A and R are true and R is the correct explanation
(B) $A$ and $R$ are true and $R$ is not the correct explanation
(C) $A$ is true but $R$ is not the correct explanation
(D) Both A and R are false.
27. The electric field given by $E(z, t)=10$ sin $(\omega t+\beta z) \bar{a}_{x}+10 \cos (\omega t+\beta z) \bar{a}_{y}$ is
(A) Plane polarized
(B) Elliptically polarized
(C) Circularly polarized
(D) Unpolarized
28. Match the following :

## Column I

I. Bohr's radius

1) $1 / 137$
II. Fine structure constant
2) 13.6 eV
III. Compton wavelength
3) $0.53 \mathrm{~A}^{\circ}$
IV. KE of electron in ground 4) $0.0242 \mathrm{~A}^{\circ}$ state of $\mathrm{H}_{2}$ atom

Choose correct matching among A, B, C, D for the row I, II, III, IV given below :

|  | I | II | III | IV |
| :--- | :--- | :--- | :--- | :--- |
| (A) | 3 | 2 | 4 | 1 |
| (B) | 3 | 1 | 4 | 2 |
| (C) | 1 | 2 | 3 | 4 |
| (D) | 2 | 4 | 1 | 3 |

29. Choose the wrong statement.
(A) Wave associated with material particle is a superposition of infinite number of plane waves with slightly differing $k$ values
(B) Eventhough the constituent waves can move with different speeds, the wave packet moves with particle velocity and hence never leaves the particle
(C) The phase velocity can be greater than speed of light
(D) Wavefunction gives the chance of locating the particle at a given instant of time and at a given location in space
30. The ratio of de-Broglie wavelength of an electron to that of proton when both of them move with the same kinetic energy is
(A) 1836
(B) $1 / 1836$
(C) $\sqrt{1836}$
(D) $1 / \sqrt{1836}$
31. The zero point energy of a linear harmonic oscillator is
(A) $h v$
(B) $(\mathrm{n}+1 / 2) \mathrm{h} v$
(C) $(1 / 2) \mathrm{h} v$
(D) $(1 / 2) \mathrm{h} \omega$
32. Choose the correct statement.
i. The expectation value of an observable whose operator does not depend on time explicitly is a constant with zero uncertainty.
ii. Eigen functions of a Hermitian operator belonging to distinct eigen values are orthogonal.
(A) $i$ is correct and $i i$ is wrong
(B) ii is correct and $i$ is wrong
(C) Both i and ii are correct
(D) Both i and ii are wrong
33. Entropy of a thermodynamics system does not change when the system is used for
(A) Conductance of heat from a hot reservoir to a cold reservoir
(B) Conversion of heat into work adiabatically
(C) Conversion of heat into internal energy isochorically
(D) Conversion of work into heat isothermally
34. Based on Maxwell thermodynamic relations and applying to specific heat equation, then
(A) $\mathrm{C}_{\mathrm{p}}-\mathrm{C}_{\mathrm{v}}=\mathrm{T}$
(B) $C_{p}-C_{v}=\left(\frac{\partial P}{\partial T}\right)_{V}$
(C) $\mathrm{C}_{\mathrm{p}}-\mathrm{C}_{\mathrm{v}}=\mathrm{RT}$
(D) $C_{p}-C_{V}=T\left(\frac{\partial P}{\partial T}\right)_{V}\left(\frac{\partial V}{\partial T}\right)_{P}$

Read the passage and answer the questions 35, 36 and 37 given below :

Every system(solid, liquid or gas) possesses a certain amount of energy. This energy is called internal energy and is usually denoted by the symbol $U$. The internal energy of a solid, liquid or gas consists of two parts (i) kinetic energy due to the motion (translational, rotational, vibrational) of the molecules (ii) potential energy due to the configuration (separation) of the molecules. The internal energy of a homogeneous system depends on its thermodynamic state i.e. on its thermodynamic coordinates $\mathrm{P}, \mathrm{V}$ and T .

Each definite state of the system possess a definite quantity of internal energy. A change in the internal energy can occur only if a transfer of energy between the system and surroundings is permitted. This can take place if (i) some work is performed on or by the system and (ii) some heat is absorbed or given out by the system.
35. In an isothermal process
(A) the temperature of the gas is not constant
(B) the gas does not take any heat from the surroundings
(C) the internal energy of the gas remains constant
(D) the pressure and volume of gas remain constant
36. In an adiabatic process
(A) the gas cannot take any heat from or give any heat to the surroundings
(B) the temperature of the gas remains constant
(C) the internal energy of the gas does not change
(D) no work is done either on the gas or by the gas
37. In a given process on an ideal gas $d w=0$ and $d Q>0$ then
(A) the temperature of the gas will decrease
(B) the temperature of the gas remains constant
(C) the internal energy of the gas will decrease
(D) the internal energy of the gas will increase
38. In case of two thermodynamic systems having molecules with chemical potentials $\mu_{1}$ with $N_{1}$ particles, $\mu_{2}$ with $N_{2}$ particles where $\mu_{1}>\mu_{2}$, if they are in thermal equilibrium initially, $\left(\theta_{1} \approx \theta_{2} \approx \theta\right)$ the thermodynamic condition of entropy change gives condition that
(A) $-\frac{1}{\theta}\left(\mu_{1}-\mu_{2}\right) \mathrm{dN}_{1}>0$
(B) $\left(\mu_{1}-\mu_{2}\right) \mathrm{dN}_{1}=0$
(C) $\left(\mu_{1}-\mu_{2}\right) d N_{1}>0$
(D) $\left(\mu_{1}-\mu_{2}\right) \mathrm{dN}_{2}<0$
39. Choose the correct statement. Statistical mechanics deals about
(A) not a particular individual movement of particles in a system
(B) it will not give information about overall behaviour of a system of many particles related to the properties of the particles themselves
(C) it helps how to find life history of one of the particles in a system
(D) it is not able to tell us the probability that the particle has a certain amount of energy at a certain moment
40. Choose the wrong statement. According to Fermi - Dirac statistics, Fermions
(A) have odd half integer spins
(B) they obey exclusion principle
(C) they have symmetric wave function
(D) only one Fermion can exist in a particular quantum state of a system
41. If $g_{m}$ and $r_{d}$ are the transconductance and drain resistance of a JFET respectively, the greatest voltage amplification that can be possible with this device can be
(A) $g_{m}$
(B) $r_{d}$
(C) $g_{m} r_{d}$
(D) $g_{m} / r_{d}$
42. Which one of the following is correct?
i. In a tunnel diode, current can be tripple valued function of voltage
ii. Tunnel diode possess negative resistance region
iii. Tunnel diodes are fabricated with very lightly doped PN junction
(A) i \& ii only are correct
(B) ii \& iii only are correct
(C) iii \& i only are correct
(D) All are correct
43. The sloping up of BJT characteristics in the active region of CE configuration is due to
(A) Thermal Runway
(B) Punch through
(C) Early effect
(D) Miller effect
44. Which one of the following is correct? Solar cells are used as source of power in earth satellite because they have
i) high efficiencies
ii) unlimited life
iii) high power capacity per weight
(A) i \&ii only are correct
(B) ii \& iii only are correct
(C) iii \& i only are correct
(D) All are correct
45. If $\alpha_{F}$ and $\alpha_{R}$ are the forward and inverted mode current gains of BJT, then
(A) $\alpha_{F}=\alpha_{R}$
(B) $\alpha_{F}<\alpha_{R}$
(C) $\alpha_{F}>\alpha_{R}$
(D) $\alpha_{F} \gg \alpha_{R}$
46. Which one of the following is correct?

LED i) is usually made from silicon
ii) emits light when forwarded biased
iii) do not require warm-up time
(A) i \&ii only are correct
(B) ii \& iii only are correct
(C) iii \& i only are correct
(D) None are correct
47. An ideal Op Amp is an ideal
(A) voltage controlled current source
(B) voltage controlled voltage source
(C) current controlled current source
(D) current controlled voltage source
48. Which one of the following is correct? Tuned amplifiers are
i. wide band amplifiers
ii. used in Radio Transmitters and Receivers
iii. performance is determined by Q of the circuit
(A) i \& ii only are correct
(B) ii \& iii only are correct
(C) iii \& i only are correct
(D) All are correct
49. In Toggle mode, JK flip flop has
(A) $\mathrm{J}=0, \mathrm{~K}=0$
(B) $\mathrm{J}=0, \mathrm{~K}=1$
(C) $\mathrm{J}=1, \mathrm{~K}=0$
(D) $\mathrm{J}=1, \mathrm{~K}=1$
50. While $\qquad$ is the fastest unsaturated logic gate, ........ has excellent noise immunity.
(A) ECL, TTL
(B) TTL, ECL
(C) ECL, HTL
(D) RTL, DTL

Space for Rough Work

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